# Internet Appendix for "Asymmetry in Stock Comovements: An Entropy Approach"

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August 2017

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This Internet Appendix describes additional analyses and tabulates additional results that are mentioned in the paper. Below, we briefly describe the contents of the appendix.

- Section IA.I: Description of bootstrap procedures for the entropy test of asymmetry as discussed in footnote 7 of the paper.
- Table IA.1: Maximum likelihood estimates for the GARCH(1,1) processes as discussed in Section III.B of the paper.
- Table IA.2: Maximum likelihood estimates for the TGARCH(1,1) processes as discussed in footnote 10 of the paper.
- Table IA.3: Size and powers for the entropy test and the HTZ test when the marginal distribution is GARCH(1,1) and the nominal size is set to 1% as discussed in Section III.B of the paper.
- Table IA.4: Size and powers for the entropy test and the HTZ test when the marginal distribution is GARCH(1,1) and the nominal size is set to 10% as discussed in Section III.B of the paper.
- Table IA.5: Size and powers for the entropy test and the HTZ test when the marginal distribution is TGARCH(1,1) and the nominal size is set to 5% as discussed in footnote 10 of the paper.
- Table IA.6: Size and powers for the entropy test and the HTZ test when the marginal distribution is TGARCH(1,1) and the nominal size is set to 1% as discussed in footnote 10 of the paper.
- Table IA.7: Size and powers for the entropy test and the HTZ test when the marginal distribution is TGARCH(1,1) and the nominal size is set to 10% as discussed in footnote 10 of the paper.
- Table IA.8: Asymmetry test results of common portfolios in shorter time periods as discussed in footnote 14 of the paper.

# IA.I Bootstrap Procedures for the Entropy Test of Asymmetry

To construct a sample under the null hypothesis of equal densities in the bootstrap resampling procedure, let

$$Z_i = \{(x_1, y_1), (x_2, y_2), \dots, (x_T, y_T); (-x_1, -y_1), (-x_{i,2}, -y_2), \dots, (-x_{i,T}, -y_T)\},\$$

which is a vector obtained by stacking together the original data pairs  $(x_i, y_i)$  with the rotated data pairs  $(-x_i, -y_i)$ . Through bootstrapping samples from  $Z_i$ , we construct the empirical distribution of  $\hat{S}_{\rho}(c)$ . We repeat the bootstrapping draws B times from  $Z_i$  and then obtain B resamples of  $\hat{S}_{\rho}(c)$ .

There are many different bootstrap resampling procedures, such as, simple bootstrap, wild bootstrap, and block bootstrap. The choice among procedures depends on the nature of the data. As stock returns are known to be stationary and weakly dependent, the block bootstrap that takes such a dependence structure into account seems to be the natural choice (Künsch (1989)). Politis and Romano (1994) show that using overlapping blocks with lengths that are randomly sampled from a geometric distribution yields stationary bootstrapped data samples, while overlapping or non-overlapping blocks with fixed lengths may not ensure such stationarity. Their procedure is known as the stationary bootstrap. Due to its favorable properties, we use it below.

The selection of the average block length *l* used in the stationary bootstrap is another important issue. We apply the data-driven and automatic method suggested by Politis and White (2004) and Patton, Politis, and White (2009) to select the optimal block length. Econometrically, this method is beneficial, since it minimizes the mean squared error of the estimated long-run variance of the time series.

In terms of selecting B, the number of bootstrap samples, it is obviously true that the greater the value of B, the more accurate the bootstrapped distribution. However, unlike the common bootstrap procedures used in linear regressions, a kernel estimation can be enormously time-consuming. In similar problems, Davidson and MacKinnon (2000) suggest the use of B = 399. In this paper, although we find that a value of B = 199 already yields similar results, we follow the suggestion of Davidson and MacKinnon (2000) and use B = 399.

After having computed B replications of  $\hat{S}_{\rho}(c)^*$ , we easily obtain the sampling distribution of  $\hat{S}_{\rho}(c)$ . To find out the critical values for rejection at different confidence levels, we reorder the bootstrapped estimates from smallest to largest and denote the list as  $\hat{S}_{\rho,1}(c)^*$ ,  $\hat{S}_{\rho,2}(c)^*$ , ...,  $\hat{S}_{\rho,B}(c)^*$ , and then determine the percentiles from these ordered statistics. For example, to conduct the symmetry test at the 5% level, the null hypothesis of equal densities will be rejected if  $\hat{S}_{\rho}(c) > \hat{S}_{\rho,379}(c)^*$ , where  $\hat{S}_{\rho,379}(c)^*$  is the 95th percentile of the ordered bootstrapped estimates. Empirical p-values are also obtained by counting the proportion of the ordered bootstrapped statistics that exceeds  $\hat{S}_{\rho}(c)$ , the test statistic estimated from the original sample.

### Table IA.1: ML Estimates for GARCH(1,1) Processes

The table reports maximum likelihood estimates for parameters of GARCH(1,1) processes used to fit the value-weighted return of the 7th smallest size portfolio (Panel A) and the value-weighted market return (Panel B) data. The GARCH models are then used as the data-generating processes to simulate the return series. The specification is set to follow a standard GARCH(1,1) process:  $r_{i,t} = \mu_i + \varepsilon_{i,t}$  where  $\varepsilon_{i,t}$  is normally distributed with a time-varying variance  $\sigma_{i,t}^2 = \omega_i + \alpha_i \varepsilon_{i,t-1}^2 + \beta_i \sigma_{i,t-1}^2$ .  $\mu_i$  is the unconditional mean for the return series.  $\omega_i$  is the constant term in the time-varying conditional volatility process.  $\alpha_i$  is the autoregressive parameter and  $\beta_i$  is the moving average parameter in the GARCH(1,1) process.

Panel A: Fitted Parameters for Value-Weighted Monthly Returns of Size 7 Portfolio

	Estimate	S.E.	t-value	p-value
$\mu_i$	0.795	0.207	3.846	0.000
$\omega_i$	2.400	1.186	2.023	0.043
$lpha_i$	0.090	0.030	3.035	0.002
$eta_i$	0.827	0.055	14.968	0.000

Panel B: Fitted Parameters for Value-Weighted Monthly Returns of Market Portfolio

	Estimate	S.E.	t-value	p-value
$\mu_i$	0.562	0.171	3.291	0.001
$\omega_i$	1.139	0.556	2.049	0.040
$lpha_i$	0.107	0.029	3.709	0.000
$oldsymbol{eta}_i$	0.844	0.036	23.231	0.000

### Table IA.2: ML Estimates for TGARCH(1,1) Processes

The table reports maximum likelihood estimates for parameters of TGARCH(1,1) processes used to fit the value-weighted return of the 7th smallest size portfolio (Panel A) and the value-weighted market return (Panel B) data. The TGARCH models are then used as the data-generating processes to simulate the return series. The specification for the marginal distribution is set to follow a TGARCH(1,1) process:  $r_{i,t} = \mu_i + \varepsilon_{i,t}$  where  $\varepsilon_{i,t}$  is normally distributed with a time-varying standard deviation  $\sigma_{i,t} = \omega_i + \alpha_i(|\varepsilon_{i,t-1}| - \gamma_i\varepsilon_{i,t-1}) + \beta_i\sigma_{i,t-1}$ .  $\mu_i$  is the unconditional mean for the return series.  $\omega_i$  is the constant term in the time-varying conditional volatility process.  $\alpha_i$  is the autoregressive parameter and  $\beta_i$  is the moving average parameter in the TGARCH(1,1) process.  $\gamma_i$  is the asymmetric response parameter that governs leverage effect in conditional volatility.

Panel A: Fitted Parameters for Value-Weighted Monthly Returns of Size 7 Portfolio

	Estimate	S.E.	t-value	p-value
$\mu_i$	0.802	0.222	3.614	0.000
$\omega_i$	0.902	0.421	2.142	0.032
$\alpha_i$	0.116	0.039	2.984	0.003
$eta_i$	0.732	0.104	7.013	0.000
$\gamma_i$	1.000	0.276	3.622	0.000

Panel B: Fitted Parameters for Value-Weighted Monthly Returns of Market Portfolio

	Estimate	S.E.	t-value	p-value
$\mu_i$	0.491	0.175	2.811	0.005
$\omega_i$	0.660	0.328	2.014	0.044
$lpha_i$	0.103	0.032	3.255	0.001
$\beta_i$	0.769	0.080	9.608	0.000
$\gamma_i$	1.000	0.393	2.547	0.011

Table IA.3: Size and Power: Entropy Test and HTZ Test

The nominal size of the tests is set to 1%. This table reports the rejection rates for the null hypothesis of symmetric comovement based on 1,000 Monte Carlo simulations. Different values of  $\kappa$  govern the degree of left tail dependence of the underlying DGP. When  $\kappa = 100\%$ , the DGP is a joint normal distribution and the rejection rates are the empirical sizes. In all other cases, the rejection rates reflect empirical power. The Clayton copula parameter  $\tau = 5.768$  and the Gaussian copula parameter  $\rho = 0.951$ . The specification for the marginal distribution is set to follow a standard GARCH(1,1) process:  $r_{i,t} = \mu_i + \varepsilon_{i,t}$  where  $\varepsilon_{i,t}$  is normally distributed with a time-varying variance  $\sigma_{i,t}^2 = \omega_i + \alpha_i \varepsilon_{i,t-1}^2 + \beta_i \sigma_{i,t-1}^2$ .  $\mu_i$  is the unconditional mean for the return series.  $\omega_i$  is the constant term in the time-varying conditional volatility process.  $\alpha_i$  is the autoregressive parameter and  $\beta_i$  is the moving average parameter in the GARCH(1,1) process.

	Ent	ropy Test	HTZ Test			
	c={0}	c={0, 0.5, 1,1.5}	c={0}	$c$ ={0, 0.5, 1,1.5}		
		<b>Panel A:</b> $\kappa = 100\%$ (	(cizo)			
T = 240	0.003	0.003	0.000	0.003		
T = 420	0.003	0.006	0.000	0.000		
T = 600	0.006	0.005	0.000	0.000		
T = 840	0.010	0.014	0.000	0.000		
		<b>Panel B:</b> $\kappa = 75\%$	6			
T = 240	0.006	0.006	0.000	0.007		
T = 420	0.027	0.018	0.000	0.003		
T = 600	0.059	0.038	0.000	0.001		
T = 840	0.126	0.062	0.000	0.000		
		Panel C: $\kappa = 50\%$	6			
T = 240	0.070	0.068	0.011	0.040		
T = 420	0.315	0.221	0.028	0.029		
T = 600	0.637	0.476	0.051	0.041		
T = 840	0.921	0.773	0.116	0.049		
		<b>Panel D:</b> $\kappa = 37.5$	%			
T = 240	0.160	0.151	0.030	0.072		
T = 420	0.627	0.512	0.097	0.086		
T = 600	0.920	0.798	0.192	0.123		
T = 840	0.987	0.955	0.390	0.186		
		Panel E: $\kappa = 25\%$	6			
T = 240	0.343	0.331	0.096	0.150		
T = 420	0.872	0.774	0.300	0.215		
T = 600	0.989	0.951	0.531	0.294		
T = 840	1.000	0.995	0.745	0.475		
		<b>Panel F:</b> $\kappa = 0\%$	)			
T = 240	0.794	0.775	0.396	0.423		
T = 420	0.991	0.980	0.780	0.627		
T = 600	1.000	1.000	0.935	0.766		
T = 840	1.000	1.000	0.986	0.917		

Table IA.4: Size and Power: Entropy Test and HTZ Test

The nominal size of the tests is set to 10%. This table reports the rejection rates for the null hypothesis of symmetric comovement based on 1,000 Monte Carlo simulations. Different values of  $\kappa$  govern the degree of left tail dependence of the underlying DGP. When  $\kappa = 100\%$ , the DGP is a joint normal distribution and the rejection rates are the empirical sizes. In all other cases, the rejection rates reflect empirical power. The Clayton copula parameter  $\tau = 5.768$  and the Gaussian copula parameter  $\rho = 0.951$ . The specification for the marginal distribution is set to follow a standard GARCH(1,1) process:  $r_{i,t} = \mu_i + \varepsilon_{i,t}$  where  $\varepsilon_{i,t}$  is normally distributed with a time-varying variance  $\sigma_{i,t}^2 = \omega_i + \alpha_i \varepsilon_{i,t-1}^2 + \beta_i \sigma_{i,t-1}^2$ .  $\mu_i$  is the unconditional mean for the return series.  $\omega_i$  is the constant term in the time-varying conditional volatility process.  $\alpha_i$  is the autoregressive parameter and  $\beta_i$  is the moving average parameter in the GARCH(1,1) process.

	Ent	ropy Test	HTZ Test			
	c={0}	c={0, 0.5, 1,1.5}	c={0}	$c$ ={0, 0.5, 1,1.5}		
		<b>Panel A:</b> $\kappa = 100\%$ (	(size)			
T = 240	0.077	0.069	0.000	0.010		
T = 420	0.083	0.099	0.000	0.000		
T = 600	0.096	0.115	0.000	0.000		
T = 840	0.113	0.123	0.000	0.001		
		<b>Panel B:</b> $\kappa = 759$	<i>%</i>			
T = 240	0.138	0.126	0.006	0.045		
T = 420	0.254	0.212	0.008	0.020		
T = 600	0.408	0.331	0.013	0.014		
T = 840	0.627	0.493	0.024	0.016		
		Panel C: $\kappa = 50^\circ$	<b>√</b> 0			
T = 240	0.454	0.429	0.168	0.165		
T = 420	0.820	0.726	0.324	0.181		
T = 600	0.969	0.917	0.508	0.221		
T = 840	0.994	0.983	0.711	0.315		
		<b>Panel D:</b> $\kappa = 37.5$	%			
T = 240	0.722	0.675	0.326	0.269		
T = 420	0.958	0.917	0.596	0.322		
T = 600	0.997	0.977	0.785	0.421		
T = 840	1.000	0.999	0.916	0.605		
		Panel E: $\kappa = 259$	<i>To</i>			
T = 240	0.882	0.857	0.578	0.435		
T = 420	0.991	0.984	0.854	0.589		
T = 600	1.000	1.000	0.953	0.723		
T = 840	1.000	1.000	0.984	0.869		
		<b>Panel F:</b> $\kappa = 0\%$				
T = 240	0.991	0.983	0.902	0.759		
T = 420	1.000	1.000	0.984	0.904		
T = 600	1.000	1.000	0.997	0.964		
T = 840	1.000	1.000	0.999	0.992		

Table IA.5: Size and Power with TGARCH(1,1) Marginals: Entropy Test and HTZ Test

The nominal size of the tests is set to 5%. This table reports the rejection rates for the null hypothesis of symmetric comovement based on 1,000 Monte Carlo simulations. Different values of  $\kappa$  govern the degree of left tail dependence of the underlying DGP. When  $\kappa = 100\%$ , the DGP is a joint normal distribution and the rejection rates are the empirical sizes. In all other cases, the rejection rates reflect empirical power. The Clayton copula parameter  $\tau = 5.768$  and the Gaussian copula parameter  $\rho = 0.951$ . The specification for the marginal distribution is set to follow a TGARCH(1,1) process:  $r_{i,t} = \mu_i + \varepsilon_{i,t}$  where  $\varepsilon_{i,t}$  is normally distributed with a time-varying standard deviation  $\sigma_{i,t} = \omega_i + \alpha_i(|\varepsilon_{i,t-1}| - \gamma_i \varepsilon_{i,t-1}) + \beta_i \sigma_{i,t-1}$ .  $\mu_i$  is the unconditional mean for the return series.  $\omega_i$  is the constant term in the time-varying conditional volatility process.  $\alpha_i$  is the autoregressive parameter and  $\beta_i$  is the moving average parameter in the TGARCH(1,1) process.  $\gamma_i$  is the asymmetric response parameter that governs leverage effect in conditional volatility.

	Ent	ropy Test	HTZ Test			
	c={0}	c={0, 0.5, 1,1.5}	c={0}	$c$ ={0, 0.5, 1,1.5}		
		<b>Panel A:</b> $\kappa = 100\%$ (	(size)			
T = 240	0.030	0.035	0.000	0.004		
T = 240 $T = 420$	0.030	0.033	0.000	0.004		
T = 600	0.043	0.047	0.000	0.002		
T = 840	0.059	0.057	0.000	0.002		
1 - 040	0.039	0.037	0.000	0.000		
		<b>Panel B:</b> $\kappa = 759$	6			
T = 240	0.080	0.080	0.001	0.017		
T = 420	0.137	0.125	0.001	0.006		
T = 600	0.257	0.213	0.002	0.002		
T = 840	0.402	0.312	0.002	0.003		
		Panel C: $\kappa = 509$	%			
T = 240	0.230	0.222	0.014	0.048		
T = 420	0.605	0.527	0.033	0.037		
T = 600	0.873	0.807	0.063	0.031		
T = 840	0.972	0.949	0.123	0.043		
		<b>Panel D:</b> $\kappa = 37.5$	%			
T = 240	0.396	0.385	0.038	0.077		
T = 420 $T = 420$	0.825	0.783	0.102	0.056		
T = 600	0.956	0.945	0.205	0.079		
T = 840	0.995	0.992	0.352	0.123		
		Panel E: $\kappa = 25\%$	<i>1</i> 6			
T = 240	0.546	0.551	0.100	0.108		
T = 420	0.926	0.917	0.212	0.128		
T = 600	0.985	0.986	0.368	0.192		
T = 840	0.997	0.997	0.565	0.300		
		<b>Panel F:</b> $\kappa = 0\%$	)			
T = 240	0.789	0.803	0.241	0.229		
T = 420	0.977	0.979	0.505	0.320		
T = 600	0.996	0.998	0.698	0.459		
T = 840	1.000	0.999	0.833	0.675		

Table IA.6: Size and Power with TGARCH(1,1) Marginals: Entropy Test and HTZ Test

The nominal size of the tests is set to 1%. This table reports the rejection rates for the null hypothesis of symmetric comovement based on 1,000 Monte Carlo simulations. Different values of  $\kappa$  govern the degree of left tail dependence of the underlying DGP. When  $\kappa = 100\%$ , the DGP is a joint normal distribution and the rejection rates are the empirical sizes. In all other cases, the rejection rates reflect empirical power. The Clayton copula parameter  $\tau = 5.768$  and the Gaussian copula parameter  $\rho = 0.951$ . The specification for the marginal distribution is set to follow a TGARCH(1,1) process:  $r_{i,t} = \mu_i + \varepsilon_{i,t}$  where  $\varepsilon_{i,t}$  is normally distributed with a time-varying standard deviation  $\sigma_{i,t} = \omega_i + \alpha_i(|\varepsilon_{i,t-1}| - \gamma_i\varepsilon_{i,t-1}) + \beta_i\sigma_{i,t-1}$ .  $\mu_i$  is the unconditional mean for the return series.  $\omega_i$  is the constant term in the time-varying conditional volatility process.  $\alpha_i$  is the autoregressive parameter and  $\beta_i$  is the moving average parameter in the TGARCH(1,1) process.  $\gamma_i$  is the asymmetric response parameter that governs leverage effect in conditional volatility.

	Ent	ropy Test	HTZ Test			
	c={0}	c={0, 0.5, 1,1.5}	c={0}	$c = \{0, 0.5, 1, 1.5\}$		
		<b>Panel A:</b> $\kappa = 100\%$	(size)			
T = 240	0.008	0.003	0.000	0.003		
T = 420	0.005	0.004	0.000	0.000		
T = 600	0.008	0.007	0.000	0.000		
T = 840	0.009	0.006	0.000	0.000		
		<b>Panel B:</b> $\kappa = 75^\circ$	%			
T = 240	0.009	0.010	0.000	0.010		
T = 420	0.025	0.021	0.000	0.002		
T = 600	0.049	0.037	0.000	0.000		
T = 840	0.118	0.069	0.000	0.000		
		Panel C: $\kappa = 50^{\circ}$	%			
T = 240	0.049	0.049	0.003	0.021		
T = 420	0.254	0.192	0.002	0.008		
T = 600	0.577	0.460	0.004	0.009		
T = 840	0.871	0.749	0.014	0.008		
		<b>Panel D:</b> $\kappa = 37.5$	5%			
T = 240	0.116	0.127	0.010	0.047		
T = 420	0.517	0.439	0.015	0.012		
T = 600	0.842	0.776	0.038	0.023		
T = 840	0.976	0.948	0.086	0.036		
		Panel E: $\kappa = 25^{\circ}$	%			
T = 240	0.240	0.249	0.015	0.057		
T = 420	0.759	0.702	0.053	0.049		
T = 600	0.958	0.925	0.132	0.065		
T = 840	0.995	0.988	0.259	0.105		
		<b>Panel F:</b> $\kappa = 0\%$	6			
T = 240	0.564	0.584	0.072	0.134		
T = 420	0.930	0.926	0.229	0.172		
T = 600	0.981	0.984	0.429	0.256		
T = 840	0.997	0.995	0.624	0.415		

Table IA.7: Size and Power with TGARCH(1,1) Marginals: Entropy Test and HTZ Test

The nominal size of the tests is set to 10%. This table reports the rejection rates for the null hypothesis of symmetric comovement based on 1,000 Monte Carlo simulations. Different values of  $\kappa$  govern the degree of left tail dependence of the underlying DGP. When  $\kappa = 100\%$ , the DGP is a joint normal distribution and the rejection rates are the empirical sizes. In all other cases, the rejection rates reflect empirical power. The Clayton copula parameter  $\tau = 5.768$  and the Gaussian copula parameter  $\rho = 0.951$ . The specification for the marginal distribution is set to follow a TGARCH(1,1) process:  $r_{i,t} = \mu_i + \varepsilon_{i,t}$  where  $\varepsilon_{i,t}$  is normally distributed with a time-varying standard deviation  $\sigma_{i,t} = \omega_i + \alpha_i(|\varepsilon_{i,t-1}| - \gamma_i \varepsilon_{i,t-1}) + \beta_i \sigma_{i,t-1}$ .  $\mu_i$  is the unconditional mean for the return series.  $\omega_i$  is the constant term in the time-varying conditional volatility process.  $\alpha_i$  is the autoregressive parameter and  $\beta_i$  is the moving average parameter in the TGARCH(1,1) process.  $\gamma_i$  is the asymmetric response parameter that governs leverage effect in conditional volatility.

	Ent	ropy Test	HTZ Test			
	c={0}	c={0, 0.5, 1,1.5}	c={0}	$c$ ={0, 0.5, 1,1.5}		
		<b>D</b> onal A. 44 1000	(ai-a)			
		Panel A: $\kappa = 100\%$	· · · · ·			
T = 240	0.083	0.088	0.000	0.007		
T = 420	0.097	0.105	0.000	0.001		
T = 600	0.124	0.136	0.000	0.002		
T = 840	0.128	0.138	0.000	0.000		
		<b>Panel B:</b> $\kappa = 75^{\circ}$	%			
T = 240	0.167	0.170	0.002	0.027		
T = 420	0.277	0.267	0.005	0.009		
T = 600	0.428	0.371	0.005	0.007		
T = 840	0.587	0.489	0.004	0.005		
		<b>Panel C:</b> $\kappa = 50^{\circ}$	%			
T = 240	0.391	0.394	0.047	0.077		
T = 420	0.759	0.703	0.092	0.058		
T = 600	0.942	0.915	0.144	0.061		
T = 840	0.991	0.977	0.276	0.086		
		<b>Panel D:</b> $\kappa = 37.5$	5%			
T = 240	0.584	0.576	0.085	0.131		
T = 420	0.916	0.893	0.215	0.094		
T = 600	0.983	0.979	0.358	0.150		
T = 840	0.998	0.998	0.543	0.223		
		<b>Panel E:</b> $\kappa = 25^{\circ}$	<b>%</b>			
T = 240	0.721	0.712	0.181	0.161		
T = 420	0.964	0.962	0.365	0.212		
T = 600	0.997	0.995	0.541	0.280		
T = 840	0.999	0.998	0.739	0.436		
		<b>Panel F:</b> $\kappa = 0\%$	ó			
T = 240	0.884	0.890	0.379	0.307		
T = 420	0.985	0.989	0.653	0.428		
T = 600	0.999	0.999	0.804	0.592		
T = 840	1.000	1.000	0.906	0.783		

Table IA.8: Testing for Asymmetry

The table reports both the test statistics and the p-values of the entropy test and the HTZ test. We use (value-weighted) monthly returns of size, book-to-market, and momentum portfolios as the test assets. The last two columns report skewness and coskewness. The sample period is from January 1965 to December 1999.

	Entropy Test				HT	Z Test		Skewness	Coskew	
	c=	{0}	$c = \{0, 0.$	5, 1,1.5}	c=	$c = \{0\}$		.5, 1,1.5}		
Portfolios	$S_{\rho} \times 100$	p-Value	$S_{\rho} \times 100$	p-Value	Test-stat	p-Value	Test-stat	p-Value	_	
Size 1	1.820	0.105	1.203	0.165	2.458	0.117	9.728	0.045	-0.274	-0.595
Size 2	1.591	0.083	1.288	0.088	0.790	0.374	0.942	0.918	-0.459	-0.585
Size 3	1.473	0.175	1.237	0.170	0.549	0.459	0.856	0.931	-0.487	-0.566
Size 4	1.280	0.221	1.070	0.190	0.339	0.560	0.584	0.965	-0.577	-0.576
Size 5	1.385	0.165	1.062	0.183	0.252	0.616	4.878	0.300	-0.633	-0.582
Size 6	1.237	0.286	0.942	0.301	0.120	0.729	3.924	0.416	-0.580	-0.540
Size 7	0.971	0.561	0.802	0.471	0.016	0.898	0.706	0.951	-0.472	-0.496
Size 8	1.015	0.454	0.839	0.429	0.023	0.878	0.401	0.982	-0.429	-0.482
Size 9	0.881	0.526	0.645	0.637	0.001	0.972	0.008	1.000	-0.333	-0.433
Size 10	0.954	0.544	0.771	0.571	0.001	0.980	0.111	0.999	-0.296	-0.423

Panel B: Book-to-Market

		Entro	py Test			HT	Z Test		Skewness	Coskew
	c=	{0}	$c = \{0, 0.$	5, 1,1.5}	c=	$c = \{0\}$		.5, 1,1.5}		
Portfolios	$S_{\rho} \times 100$	p-Value	$S_{\rho} \times 100$	p-Value	Test-stat	p-Value	Test-stat	p-Value	_	
B/M 1	0.820	0.516	0.668	0.501	0.022	0.883	0.341	0.987	-0.137	-0.370
B/M 2	0.928	0.391	0.785	0.313	0.020	0.887	0.208	0.995	-0.437	-0.479
B/M 3	0.704	0.739	0.552	0.754	0.042	0.837	0.251	0.993	-0.573	-0.527
B/M 4	1.054	0.411	0.886	0.363	0.117	0.733	1.716	0.788	-0.390	-0.494
B/M 5	1.164	0.451	0.909	0.398	0.167	0.683	2.638	0.620	-0.443	-0.517
B/M 6	0.866	0.714	0.734	0.694	0.102	0.749	1.500	0.827	-0.410	-0.490
B/M 7	1.410	0.356	1.208	0.303	0.121	0.728	1.008	0.909	0.039	-0.354
B/M 8	1.523	0.185	1.256	0.163	0.278	0.598	2.570	0.632	-0.016	-0.419
B/M 9	1.623	0.183	1.333	0.140	0.504	0.478	1.180	0.881	-0.144	-0.471
B/M 10	1.420	0.308	1.046	0.343	0.588	0.443	2.896	0.575	0.086	-0.421

Panal	c.	Momentum
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	Entropy Test					HTZ Test				Coskew
	$c=\{0\}$		$c = \{0, 0.$	$c$ ={0, 0.5, 1,1.5}		$c = \{0\}$		$c$ ={0, 0.5, 1,1.5}		
Portfolios	$S_{\rho} \times 100$	p-Value	$S_{\rho} \times 100$	p-Value	Test-stat	p-Value	Test-stat	p-Value	_	
L	1.760	0.078	1.327	0.075	2.162	0.141	4.449	0.349	0.239	-0.337
2	1.415	0.429	1.037	0.531	1.231	0.267	3.009	0.556	0.079	-0.270
3	1.689	0.268	1.235	0.333	0.946	0.331	4.572	0.334	0.195	-0.255
4	1.280	0.253	0.957	0.273	0.758	0.384	4.412	0.353	-0.127	-0.377
5	1.203	0.479	0.937	0.539	0.694	0.405	4.088	0.394	-0.438	-0.506
6	1.290	0.238	0.993	0.243	0.722	0.396	0.794	0.939	-0.403	-0.523
7	1.237	0.168	1.056	0.115	0.585	0.444	3.445	0.486	-0.493	-0.526
8	0.874	0.692	0.720	0.634	0.670	0.413	0.911	0.923	-0.331	-0.449
9	1.417	0.080	1.145	0.100	1.088	0.297	1.636	0.802	-0.622	-0.558
W	2.242	0.005	1.767	0.008	1.648	0.199	10.266	0.036	-0.416	-0.492

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